Magnetic diffusion anomaly at the Néel temperature of pyrrhotite, Fe$_{1-x}$S

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Cation diffusion is an important rate-limiting process in the growth of pyrrhotite (Fe$_{1-x}$S) in passivating films on steels exposed to sulfidic environments, and for proposed synthetic applications of Fe$_{1-x}$S, for example single-phase magnetic switching devices. Above the Néel temperature $T_N$ of 315 °C, where Fe$_{1-x}$S is paramagnetic and structurally disordered, iron self-diffusivity $D_{Fe}$ predictably follows a standard, established Arrhenius law with temperature. However, we report $^{57}$Fe tracer diffusion measurements below $T_N$ obtained using secondary ion mass spectrometry (SIMS), that demonstrate a 100-fold reduction in diffusion coefficient as compared to the extrapolated, paramagnetic Arrhenius trend at 150 °C. The results can be described by a magnetic diffusion anomaly, where the vacancy migration energy for the spontaneously-magnetized cation sublattice is increased by approximately 40% over the paramagnetic state. These constitute the first set of consistent diffusivity data obtained in magnetic pyrrhotite, allowing more accurate prediction of pyrrhotite growth rates and determination of magnetic properties for synthetic devices.

1 Introduction

Pyrrhotite (Fe$_{1-x}$S) barrier layers are important in passively protecting steels against highly sulfidizing and aggressive atmospheres, encountered in energy systems where hydrogen sulfide is present, such as oil and gas production and refining. One of the key protective qualities of pyrrhotite is to limit the rate of mass transport and hence general corrosion.$^{1,2}$ Moreover, there has been recent interest in chemically fabricating low-dimensional, synthetic Fe$_{1-x}$S such as nanowires$^{3,4}$ and nanodisks$^{5}$ via solvothermal or electrodeposition methods. Such nanostructured Fe$_{1-x}$S crystals are promising for magnetic recording devices, in which the switching of magnetic states is controlled by cation-diffusion driven phase transformations.$^6$ Ionic-diffusion-driven solid state reactions have also been used to create heteroanustructures of CuS$_2$ with Fe and Zn.$^7$ In all of these cases, an accurate knowledge of Fe diffusivities in Fe$_{1-x}$S, as the key kinetic rate-limiting process in crystal growth or phase switching, is crucial to the design and prediction of the desired properties.

Fe$_{1-x}$S is an off-stoichiometric phase (0 ≤ x ≤ 0.125) which is paramagnetic and structurally disordered above its critical Néel temperature $T_N$ of 315 °C.$^8$ Below $T_N$, Fe$_{1-x}$S undergoes spontaneous magnetic ordering whereby co-planar Fe atoms normal to the crystal c-axis couple ferromagnetically and those in adjacent planes couple antiferromagnetically. Vacancy–vacancy interactions further lead to the formation of composition-dependent, ordered superstructures at low temperatures that govern overall, macroscopic magnetic properties.$^9$ Previous measurements of Fe self-diffusion $D_{Fe}$ in paramagnetic Fe$_{1-x}$S have been carried out by several authors using thermogravimetric$^{10–12}$ and radio-tracer$^{13,14}$ methods, as compiled in Fig. 1a. An isothermal spread in $D_{Fe}$ of approximately one order of magnitude is observed, stemming from variations in stoichiometry (Fig. 1a) or crystal anisotropy (Fig. 1b). Despite this, the results above ~320 °C follow a standard Arrhenius law as a function of temperature, given by $D = D_0 \exp[-Q_a/k_B T]$, where $D_0$ is a prefactor, $Q_a$ is the activation energy for diffusion in the paramagnetic lattice, and $k_B$ is Boltzmann’s constant. Stoichiometry and anisotropy influence only $D_0$.

However, Condit $et$ al. predicted decades ago that vacancy ordering below $T_N$ would lead to an increase in the activation barrier for Fe self-diffusion.$^{14}$ Indeed, the only available $D_{Fe}$ measurements at temperatures lower than ~300 °C, obtained via a unique magnetokinetic method (Fig. 1a, data labelled “Z”), may substantiate this claim but for lack of auxiliary...
supporting data. In a separate study, we recently repeated these measurements and demonstrated them to be inaccurate. Nevertheless, the influence of the simultaneous magnetic/structural order–disorder transition at $T_N$ on the diffusion coefficient of Fe in pyrrhotite remains an open question. An abrupt and discontinuous drop in $D$ at a critical temperature is commonly observed in systems that undergo structural order–disorder transitions, due to a reduction in the concentration of mobile defects, for example in oxides such as Bi$_2$O$_3$ or La$_2$Mo$_2$O$_7$.16 On the other hand a more subtle, second-order change in the Arrhenius dependence of $D$, due to a change in the migration barrier energy, is seen in ferromagnets such as body-centered cubic iron, below their spontaneous magnetic ordering or Curie temperature $T_C$.17–19

Given the primary motivation to investigate the effect of the critical ordering temperature $T_N$ on cation self-diffusion in pyrrhotite, we employed dynamic secondary ion mass spectrometry (SIMS) to measure diffusion profiles of the stable $^{57}$Fe isotope tracer in Fe$_{1-x}$S. SIMS is a highly sensitive technique that permits depth profiling on the order of nanometers and hence allowed the use of very short annealing times and low temperatures in the range 170–400 °C. Our results above $T_N$ are consistent with previous measurements obtained on disordered pyrrhotites with similar stoichiometry. In the ordered regime below $\sim$315 °C, however, our $D_{Fe}$ results fall substantially below the extrapolated trend from the disordered pyrrhotite regime. Rather than vacancy ordering, we believe that the primary effect of spontaneous magnetic ordering at $T_N$ causes this deviation in self-diffusivity. Based on a theoretical consideration of the influence of magnetic energy on vacancy formation and migration energies, we show that the activation energy $Q_M$ for diffusion in fully, magnetically-ordered pyrrhotite is up to 41% higher than $Q_P$.

2 Methods

Sample preparation

Research-grade natural crystals of pyrrhotite were obtained from Ward’s Science (Rochester, NY). Individual specimens had dimensions of approximately 5 x 5 x 5 mm$^3$ and were sourced from North Bend, WA. A representative sample of several individual crystals from the package was ground together into a powder in a porcelain mortar for XRD phase identification (Fig. 2a). Hexagonal pyrrhotite was found to be the only phase present (Inorganic Crystal Structure Database Ref. 00-050-1788). The position of the (102) peak was used to estimate an average composition of 48.0 at% Fe, corresponding approximately to Fe$_{10}$S$_{12}$ (6C), or equivalently $x$ = 0.04.21

The chemical composition of the natural crystals was investigated using energy-dispersive X-ray spectroscopy (EDS) in a JEOL 6610LV scanning electron microscope (SEM), to check for any large inclusions that may affect the reliability of the diffusion studies.† Potential metallic impurities such as Si and Al were not identified within the detection limit of the instrument (approx. 0.1 wt%),22 implying that any small inclusions were likely iron oxides. These were deemed sparse enough to not affect greatly the accuracy of the subsequent diffusion studies. The self-diffusion coefficient of iron in Fe$_2$O$_3$ is very small below 500 °C ($10^{-28}$ cm$^2$ s$^{-1}$),23 so minor ironoxide inclusions were not expected to significantly influence Fe diffusion profiles. As-received crystals

![Fig. 1](Reported Fe self-diffusivity values. (a) Experimental $D_{Fe}$ obtained using different techniques as listed. The aim of the current work was to measure a reliable set of data below 300 °C. (b) Detail from region ‘X’ on the main graph. Variations in stoichiometry $x$ account for up to one order of magnitude variation in $D_{Fe}$. (c) Detail from region ‘Y’: crystallographic anisotropy can account for half an order of magnitude variation. Data from: Fryt$^1$, Worrell$^1$, Sterten$^1$, Hobbins$^1$, Condit$^1$, Marusak$^1$,20 († = sulfurization; ‡ = radiotracer; § = magnetokinetic measurements.)}
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were polished down to 4000 grit sandpaper to achieve a flat surfaces followed by an extended polish of 5–10 min using 50 nm Al₂O₃ suspension. The resulting average surface root mean square (RMS) roughness, as measured by atomic force microscopy (AFM) was ≤50 nm.

Temperature-dependent magnetization studies confirmed that the natural pyrrhotite samples were antiferromagnetically ordered at room temperature. These samples also exhibited a peak-like, ferrimagnetic λ-transition starting at 160 °C, followed by a full magnetic disordering to a paramagnetic state at ~315 °C.† Differential scanning calorimetry (DSC), shown in (Fig. 2b), demonstrated that a reversible, exothermic release of ~5 J g⁻¹ at 316 °C, which we attribute to a first-order, spontaneous disordering of vacancies upon loss of magnetic interactions at Tᵣ.

**57Fe deposition and diffusion annealing**

To study iron self-diffusion, the stable isotope ⁵⁷Fe was used as a tracer. ⁵⁷Fe has an abundance in natural iron of approximately 2%.²⁴ Solid chips of ⁵⁷Fe (96.06% enriched, Nakima Ltd, Israel) comprising a total mass of 200 mg were evaporated onto the surface of ~40 polished Fe₁₋₅S crystals simultaneously using a Sharon TE-1 thermal evaporator. The resulting deposit thickness, measured in situ with a quartz crystal microbalance and confirmed ex situ by measuring a deposit shadow profile on a glass substrate, was 130 nm. Once coated in 130 nm of ⁵⁷Fe, pyrrhotite crystals were subjected to diffusion annealing runs at a range of temperatures between 170–400 °C for different lengths of time. Preliminary studies on synthetic thin film samples found that even small quantities of residual oxygen present during the annealing process had the effect of reducing the measured diffusivity by several orders of magnitude below expected values, due to the formation of an oxide film that tied up ⁵⁷Fe at the surface. Therefore, all bulk sample annealing was conducted in a horizontal quartz tube furnace under an O₂-free, dynamic H₂S:H₂ atmosphere in a molar ratio of 1:3500, which is within the sulfur partial pressure stability window for Fe₁₋₅S for the relevant range of temperatures.²⁵ Maintaining this reducing atmosphere prohibited the formation of oxide on the deposit or oxidation of the crystals themselves. Crystals were inserted into the hot section of the furnace for a predetermined duration before being removed outside the tube furnace for cooling under flowing H₂S/H₂. A thermocouple allowed in situ temperature profiles to be recorded for each annealing run.

**Secondary ion mass spectrometry (SIMS)**

Depth profiling of annealed specimens was conducted in a CAMECA IMS-5f dynamic SIMS at the Materials Research Laboratory of the University of Illinois (Urbana-Champaign, IL). SIMS profiling to measure diffusivity has been shown to accurately replicate bulk self-diffusion results from traditional radiotracer measurement techniques for hematite, Fe₂O₃ single crystals.²³ ⁵⁷Fe and ⁵⁶Fe depth profiles were established by using a 10 keV O⁻ primary ion beam. In addition to these two species, the instrument was calibrated to detect any metallic impurity elements (mainly Si, Al, Ca, Mg) during each measurement. Only areas of the samples where the signal from these impurities was below the detection limit of 10 ppm were used for diffusion analysis. Anions such as sulfur and oxygen could not be simultaneously measured along with cations using the O⁻ primary beam, and we do not include an analysis of these species in this work. The ⁵⁷Fe concentration [⁵⁷Fe] as a function of sputtering time was determined from the intensities I of the secondary positive ions ⁵⁶Fe⁺ and ⁵⁷Fe⁺ using:

\[ [^{57}\text{Fe}] = \frac{I(^{57}\text{Fe})}{I(^{57}\text{Fe}) + I(^{56}\text{Fe})} \]  

Conversion of sputtering time to profile depth was achieved by measuring the depth of the SIMS craters using a Dektak profiler and assuming a constant sputtering rate.²⁶ Diffusion profiles were fit to appropriate error function solutions discussed below, using MATLAB R2012b.

**3 Results and discussion**

**Fitting of diffusion profiles**

Fig. 3 compares the [⁵⁷Fe] diffusion profile of an unannealed sample with the original ⁵⁷Fe deposit versus a typical profile of an annealed sample (275 °C, 5 minutes). The original SIMS spectra as a function of time for the annealed sample are inset in the figure. The unannealed profile contains a sharp interface between the original ⁵⁷Fe deposit and the Fe₁₋₅S crystal,
located at 130 nm depth. After annealing, a $^{57}$Fe tail from diffusion extends approximately 800 nm into the crystal. Nevertheless, even after diffusion annealing at 275 °C, a substantial proportion of the initial, pure $^{57}$Fe remained on the Fe$_{1-x}$S surface. This essentially acted as a semi-infinite source of isotopic iron in the limit of the relatively short annealing times used in this work. We can therefore assume the concentration at the diffusion couple interface (i.e., at 130 nm depth) is fixed at $c = c_0$ for the duration of the annealing run. The initial and boundary conditions are hence:

$$c(x, t = 0) = 0$$ (2)

and:

$$c(x = 0, t) = c_0$$ (3)

Then it can be shown there exists an error function solution to Fick's second law in the form:26

$$c(x, t) = c_0 \left[1 - \text{erf} \left( \frac{x}{4Dt} \right) \right]$$ (4)

The diffusion tails beyond the 130 nm original deposit were normalized to an initial, interfacial concentration $c_0 = 1$ and fit using eqn (4). Fig. 4 shows an example of fitting two profiles from samples annealed at the same temperature of 225 °C but for different times of $1.8 \times 10^3$ and $1.3 \times 10^4$ s. The sample annealed longer exhibited a $^{57}$Fe profile that extends further into the sample, as expected. However, the measured $^*$D$_{Fe}$ values from fitting were similar: 4.6 and $3.4 \times 10^{-13}$, respectively. Wherever possible, more than one measurement at a single temperature was obtained to check for consistency. The best-fit error function solutions are overlaid on top of experimental data with a range of uncertainty in Fig. 4.†

**Increased diffusion activation energy from spontaneous magnetization**

Values of $^*$D$_{Fe}$ obtained from error function fitting are shown in Arrhenius form in Fig. 5, alongside representative literature results from Fryt et al.$^{10}$ and Condit et al.$^{14}$ whose data are also displayed in Fig. 1.† We include for comparison only those data corresponding to the stoichiometry range $0.03 \leq x \leq 0.1$ in Fe$_{1-x}$S, which is close to the composition of our samples analyzed via SIMS. Above $\sim 315$ °C, our measurements are consistent with the previous results, corresponding to an activation energy $Q_p = 0.83 \pm 0.03$ eV, representing the mean and standard deviation slopes obtained by regression fitting.

From Fig. 5, we also observe that below $T_N$ our $^*$D$_{Fe}$ values are considerably lower than the extrapolated Arrhenius trend with a slope of $-Q_p/k_b$. A deviation of this type beginning around 300 °C was previously observed by Condit et al., who postulated that vacancy ordering reduced the number of mobile vacancies by fixing Fe vacancies in equilibrium superlattice positions, characterized by long residence times. Despite this observation, their experiments were not pursued to low enough temperatures to confirm this hypothesis or to quantify the activation energy in the new regime. In this study, we also considered the possibility that vacancy ordering may produce the observed, anomalous behavior at $T \leq T_N$. By comparison, however, oxides that undergo structural order–disorder transitions display large, discontinuous drops in diffusivity, by up to several orders of magnitude, at the critical ordering temperature.16 Conversely, the change in Arrhenius behavior of $^*$D$_{Fe}$ in Fig. 5 is continuous and does not seem to be consistent with the expected effect of a first-order structural reorganization. Rather, the transition is more reminiscent of the so-called “magnetic diffusion anomaly” observed at the paramagnetic–ferromagnetic critical point or Curie temperature $T_C$ in ferromagnetic materials. Self-diffusion$^{19,27,28}$ and solute diffusion$^{18,29}$ in Fe, interdiffusion in Fe–Ni alloys$^{30}$ and, to a lesser extent, diffusion in Co$^{19}$ all

![Fig. 3](image-url) The interdiffusion of a 130 nm-thick $^{57}$Fe deposit on Fe$_{1-x}$S crystals was measured by secondary ion mass spectrometry (SIMS). The black curve shows the SIMS profile from an unannealed sample, indicating the depth of the original deposit. Inset: raw SIMS data for a sample annealed for 5 minutes at 275 °C, converted in the main plot to $^{57}$Fe concentration vs. depth into the crystal (grey curve).

![Fig. 4](image-url) The tail of each diffusion profile was fit with an error function solution (eqn (4)). Example fits for two samples annealed at 225 °C for approx. 1800 and 13 000 s are shown.
display a deviation from the Arrhenius law extrapolated from the paramagnetic region at \( T_C \), characterized by a sharp spike or discontinuity in the effective activation energy \( Q_{\text{eff}} \) given by:

\[
Q_{\text{eff}} = -k_B \frac{d(\ln D(T))}{d(1/T)}
\]

In other words, the magnetic transition has a second-order effect on \( D \), manifested in an abrupt change in Arrhenius slope. Ruch et al. derived a theoretical model for the magnetic diffusion anomaly, based on a constant diffusivity prefactor \( D_0 \) and a magnetic contribution to the activation energy for diffusion that varies with temperature as \( S(T)^2 \), where \( S \) is the reduced magnetization relative to magnetization at zero Kelvin: \( S(T) = M(T)/M(T = 0 \text{ K}) \). The generic diffusion coefficient in a magnetically ordered system can be written:

\[
D(T) = D_0 \exp \left[ -\frac{Q_p(1 + zS(T)^2)}{k_B T} \right]
\]

where the factor \( z \) includes the additive influence of magnetism on vacancy formation and migration energies. The \( *D_{Fe} \) data in Fig. 5 are fit to eqn (6) using the temperature variation of the \( \{001\}_{\text{bulk}} \) magnetic reflection in synthetic Fe-S-Si obtained by Powell et al. The factor \( z \) thus quantifies the magnetic ordering effect on the vacancy formation and migration energies, leading to an effective ferromagnetic activation energy for diffusion \( Q_{\text{M}} = Q_p + zS(T)^2 \). From our results we obtained a best fit of \( z = 0.41 \pm 0.06 \). In other words, the activation energy for diffusion at maximum magnetization \( (0 \text{ K}) \) is approximately \( 1.18-1.30 \text{ eV} \), as opposed to \( 0.83 \text{ eV} \) in the paramagnetic crystal at high temperatures. Additional fitting details are provided in the ESL. We assume here that the vacancy concentration remained fixed at the original bulk value of \( C_V = 0.04 \) during the annealing experiments. In other words, the effectively semi-infinite sample into which the Fe-57 exchanged remained at fixed stoichiometry. In this case, the increase in overall diffusion activation energy can be attributed solely to the magnetic influence on migration barrier.

Nevertheless, it is worth adding a small comment regarding the reliability of our results as pure self-diffusivity measurements. Since Fe-57 was used as the tracer exchange material on top of the iron sulfide specimens, a small extent of chemical diffusion undoubtedly would have affected the measured diffusion profiles. The chemical contribution to diffusion arises from a small concentration gradient developing during annealing, altering the stoichiometry in the topmost, interdiffused volume towards a Fe:Si ratio of 1:1. Such a chemical diffusion component would thus be expected to increase the diffusion rate and hence lead to a slight overestimate in self-diffusion values \( *D_{Fe} \). We did not quantify the extent of chemical diffusion contribution directly in our analysis, but, judging by the overlap of our data with the literature values in Fig. 5, it is likely to be small. Moreover, any unintended but systematic overestimate in \( D_{Fe} \) does not change the key observation of a magnetic diffusion anomaly, which leads to values considerably lower than the extrapolated, paramagnetic trend with temperature.

The implications of the magnetic diffusion anomaly in pyrrhotite are twofold. First, the growth conditions for Fe\(_{1-x}\)S in solution both as a by-product of H\(_2\)S corrosion on iron and steels in energy infrastructure, as well as intentionally via solvothermal
or electrodeposition methods for potential synthetic applications, are typically below 300 °C. Therefore any \textit{a priori} prediction of pyrrhotite growth rates from a consideration of cation diffusion must account for the effect of spontaneous magnetization, which reduces $^*D_{Fe}$ by up to 100-fold at 150 °C when compared to a linear extrapolation of the Arrhenius slope from above the spontaneous ordering temperature. The accuracy of predictive tools for H$_2$S corrosion as well as more careful control of Fe$_{1-x}$S nanocrystal synthesis both stand to benefit from these findings. Second, although Fe$_{1-x}$S has long been studied for its interesting magnetic properties, to the authors’ knowledge there is no example of a successful technological implementation of this material. Since the magnetic switching phenomena of interest in Fe$_{1-x}$S involve the local, diffusive rearrangement of vacancies, knowing the activation energy for Fe vacancy migration and formation in the magnetized state permits the development of simulation tools to design useful devices from this material, such as temperature- and/or electric field-driven magnetic switching and memory applications.

4 Conclusions

In conclusion, $^{57}$Fe tracer diffusion measurements were conducted to determine iron self-diffusivity $^*D_{Fe}$ in Fe$_{1-x}$S as a function of temperature in the range 170–400 °C, which extends across the known magnetostuctural order–disorder transition temperature $T_N = 315$ °C. Our results for $^*D_{Fe}$ above $T_N$ agree well with measurements from previous studies in paramagnetic and structurally-disordered pyrrhotite, with an activation energy $Q_V = 0.83$ eV. However, below $T_N$ iron self-diffusivity deviates downwards from the extrapolated paramagnetic Arrhenius trend by approximately a factor of 10 at 200 °C and a factor of 100 at 150 °C. This can be rationalized by considering a magnetic ordering effect on Fe vacancy migration energy, which increases the overall diffusion activation energy by up to 41% or to approximately 1.18–1.30 eV in the fully magnetically ordered state. To our knowledge, this work constitutes the first description of a magnetic contribution to diffusivity allows more accurate crystal growth rate measurements from previous studies in paramagnetic and structurally-disordered pyrrhotite.

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