Diffusion-limited kinetics of the antiferromagnetic to ferrimagnetic \( \lambda \)-transition in Fe\(_{1-x}\)S

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Fe\(_{1-x}\)S (0.08 \( \leq x \leq 0.11 \)) exhibits a simultaneous magneto-structural “\( \lambda \)-transition” at approximately 200°C. Time-dependent magnetization measurements demonstrate the \( \lambda \)-transition can be accurately modeled by a stretched exponential function, consistent with a nucleation-free, continuous reordering of the vacancy-bearing sublattice. The experimental result is supported by kinetic Monte Carlo simulations that confirm the activation energy for the transition to be 1.1 ± 0.1 eV—representing the iron vacancy migration energy in ordered Fe\(_{1-x}\)S. A mechanistic understanding of the \( \lambda \)-transition enables potential functional uses of Fe\(_{1-x}\)S such as thermally activated magnetic memory, switches, or storage. © 2015 AIP Publishing LLC [http://dx.doi.org/10.1063/1.4913201]

Pyrrophitites are a set of cation-deficient iron monosulfides across the narrow composition range 0 \( \leq x \leq 0.125 \) in Fe\(_{1-x}\)S. The unusual magnetic properties of pyrrhotite have long been studied for their fundamental interest. Recently, Fe\(_{1-x}\)S nanowires\(^1,2\) and nanodisks\(^3\) that display an antiferromagnetic (AF) to ferrimagnetic (FI) “\( \lambda \)-transition” upon heating have been investigated and proposed for technological purposes such as phase-change magnetic memory devices.\(^4\) Fe\(_{1-x}\)S is known to display independent ferroelectric\(^5\) and local ferromagnetic properties, depending on composition, suggesting it may be a candidate single-phase multiferroic material,\(^6\) similar to NiS,\(^7\) CuCrS\(_2\),\(^8\) and AgCrS\(_2\).\(^9\) In this regard, Fe\(_{1-x}\)S presents a low cost, non-toxic, and earth-abundant option. However, there remains considerable confusion regarding the mechanisms of the magnetic transitions in pyrrhotite, including the origin of the \( \lambda \)-transition. Prior attempts to quantify the AF-FI transformation kinetics assumed simple, exponential kinetics that fail to capture adequately the underlying atomic-scale lattice rearrangements.\(^10,11\)

First, we briefly review the atomic scale structural changes associated with the \( \lambda \)-transition, aided by the phase diagram in Figure 1(a). The basic unit cell for all Fe\(_{1-x}\)S compositions is NiAs-type hexagonal with the space group \( P6_2c \). Below a common magnetic ordering (Néel) temperature \( T_N \) of 320°C, Fe\(_{1-x}\)S forms a series of complex, structurally ordered polytypes based on Kagome nets, minimizing total vacancy-vacancy interaction energy.\(^12\) The superstructures are defined by a periodicity of full- and partially vacant Fe atom layers, stacked along the \( c \)-axis. In-plane, Fe atoms are aligned ferromagnetically (\( \uparrow \uparrow \uparrow \uparrow \)), whereas AF (\( \uparrow \downarrow \downarrow \uparrow \downarrow \)) coupling arises between adjacent layers.\(^11\) The presence of iron vacancies on any given \( a-b \) plane reduces the overall ferromagnetic moment; net magnetism is hence determined by the symmetry of layer occupancy. For example, “4C” pyrrhotite (Fe\(_{1-x}\)S; \( x = 0.125 \pm 0.05 \)) adopts a monoclinic structure in which the cation layers alternate between full and quarter-vacant, resulting in net ferrimagnetism (Fig. 1(b)).\(^13\) In the composition range 0.08 \( \leq x \leq 0.11 \), on the other hand, Fe\(_{1-x}\)S forms a set of AF, hexagonal superstructures known collectively as “NC,” \( 5 \leq N \leq 11 \) (e.g., Fig. 1(c)).\(^14\) The temperature-dependent magnetization \( \sigma(T) \) of AF, NC-ordered pyrrhotites is characterized by the appearance of a peak during heating, centered around 210°C, believed to arise from a diffusive structural rearrangement towards an FI superlattice (\( \lambda \)-transition).\(^15\)

An initial attempt to replicate the earlier kinetic experiments of Marusak et al.\(^11\) revealed a more complex time-evolution of the ferrimagnetic superlattice than previously appreciated. Instead of a simple exponential fit, we demonstrate the magnetokinetics are better modeled by a phenomenological, stretched exponential function of the form

\[
\tau(t) = 1 - \exp\left(-\frac{t}{\tau}\right)^n,
\]

where \( \tau \) describes a temperature-dependent relaxation time, and \( n = 0.45 \pm 0.05 \). Moreover, we conducted kinetic Monte Carlo (kMC) simulations of the \( \lambda \)-transition that reproduced the structural evolution on the experimental timescale from an AF to FI lattice under cation vacancy diffusion alone. The kMC results similarly give a stretched exponential time dependence and help understand the transition as a continuous-ordering transformation. A physical basis for the stretched exponential form of the kinetics is discussed. Finally, we show the temperature dependence of \( \tau \) in Eq. (1) yields an activation energy of 1.1 ± 0.1 eV for the \( \lambda \)-transition, which can be taken as the migration energy for cation diffusion in ordered pyrrhotite.
FeS$_7$ (4C), Fe$_{10}$S$_{11}$ (11C), and Fe$_{11}$S$_{12}$ (6C) pyrrhotite samples were prepared by reacting the requisite amounts of high-purity iron and sulfur powders in vacuum-sealed quartz tubes. Magnetic measurements were obtained using a variable-temperature Vibrating Sample Magnetometer (VSM) under a flowing N$_2$ atmosphere and an applied field of 10 kOe.

Temperature-dependent magnetization $\sigma(T)$ results for the 4C, 11C, and 6C Fe$_{17}$-S samples are shown in Figure 2. The 4C pyrrhotite followed reversible FI, Weiss-type behavior as expected up to $T_N = 320$°C (Fig. 2(a)). However, the 11C and 6C displayed markedly different $\sigma(T)$ behavior (Figs. 2(b) and 2(c)). On the first heating cycle, labelled (1) in the figures, $\sigma$ started close to 0 emu/g, consistent with AF ordering. The $\lambda$-transition peak was observed starting around 180°C, with a maximum at 210°C. However, during the cooling portion of the cycle from 350°C, the peak was not reproduced and $\sigma$ increased with Weiss behavior back to room temperature. Multiple, repeated heating/cooling cycles (2–5) as indicated on the curves only served to increase overall magnetization further. The maximum room temperature magnetization $\sigma_{RT}$ reached by 11C after several experimental cycles ($\sim$13 emu/g) was greater than that of the 6C sample ($\sim$10 emu/g); neither reached the maximum of the 4C sample ($\sigma_{RT} \sim$ 22 emu/g). Thus, the final $\sigma$ for a given structure is limited by the availability of iron vacancies $V_{Fe}$ to maximize the magnetic asymmetry between vacancy-bearing and full layers.

To understand the transformation kinetics in more detail, we performed isothermal, $\sigma(t)$ measurements on samples of 11C between 140–220°C. Assuming $V_{Fe}$ diffusion-driven exponential growth in $\sigma$ during the $\lambda$-transition, iron self-diffusion coefficients on the order of $10^{-17}$ cm$^2$/s have been found by magnetokinetic methods within this transition temperature range that are inconsistently low compared to extrapolated diffusivities obtained from high-temperature sulfidation and radiotracer diffusion studies ($O(10^{-14}$ cm$^2$/s)). However, we found that our magnetokinetic data were more accurately described by the stretched exponential function in Eq. (1).

We first converted experimental $\sigma$ to “phase fraction” of FI ordering, $x_{FI}$, according to

$$x_{FI} = \frac{\sigma_f - \sigma_i}{\sigma_f - \sigma_i},$$

where $\sigma_i$ is the measured magnetization at time $t$, $\sigma_i$ is initial magnetization at $t = 0$, and $\sigma_f$ is final magnetization assuming the transition were allowed to proceed to completion. $\sigma_f$ values for the different temperatures were therefore obtained.

![FIG. 1. (a) Fe-S phase diagram in the composition range 0 ≤ $\alpha$ ≤ 0.125 in Fe$_{17}$-S, showing the existence range of the different pyrrhotite polytypes. Exponentially determined temperatures for the $\alpha$, $\beta$- and $\lambda$-transition onsets ($T_\alpha$, $T_\beta$, and $T_\lambda$), respectively, are also shown. (b) Equilibrium Fe$_{17}$-S 4C superstructure with alternating full and partially vacant occupancy of AB-layers. An uncompensated magnetic moment results in net antiferromagnetism. “F” refers to full Fe layers; A–D are vacancy-bearing layers with different in-plane vacancy arrangements. (b) Idealized 5C superstructure with net magnetic compensation between full and vacancy-bearing layers; net antiferromagnetism.

![FIG. 2. Temperature-dependent magnetization $\sigma(T)$ for: (a) 4C, (b) 11C, and (c) 6C pyrrhotite samples. Multiple consecutive forward and reverse sweeps between 30 and 330°C, as labelled 1–5 on each of the graphs, were performed until no change from the previous sweep was observed. On (b) and (c) the inset graphs show a magnified region around the peak observed on the first sweep. The heating and cooling rates were both 0.2°C/min; the applied field was 10 kOe.]
from curve number (4) in Fig. 2(b), i.e., the maximum FI magnetization.

The experimental data were complemented by kMC simulations (full details in Ref. 14), based on the probability \( P \) of a diffusive vacancy jump, given by: (i) the intrinsic activation barrier to migration \( E_m \); (ii) an energy bias, \( E_{\text{therm}} \), due to a thermodynamic driving force towards ordering; and (iii) a bias due to the magnetic energy, \( E_{\text{mag}} \). 

\[
P = \nu \exp \left[ -\frac{E_m}{k_B T} \right] \exp \left[ -\frac{E_{\text{therm}}}{k_B T} \right] \exp \left[ -\frac{E_{\text{mag}}}{k_B T} \right], \tag{3}
\]

where \( k_B \) is Boltzmann’s constant. The energy barrier \( E_m \) was taken to be 1.2 eV, as calculated from Density Functional Theory.\(^{14}\) The energy term \( E_{\text{therm}} \) was based on thermodynamic data for pyrrhotite polytypes.\(^{22}\) Subsequent to each diffusive jump, an order parameter \( \Theta \) was assigned to the updated structure, based on the root mean squared (RMS) difference from the periodically alternating occupancy of a perfectly vacancy-segregated superstructure. Net magnetization \( \sigma \) was evaluated by summing over all individual magnetic moments on lattice sites.

Figures 3(a) and 3(b) show the results for the experimental and simulated \( \lambda \)-transition magnetokinetics, with \( n = 0.45 \pm 0.05 \) and 0.67 \( \pm \) 0.05, respectively (sensitivity analysis in Ref. 14). Nevertheless, the KMC model, based solely on cation diffusion, accurately replicates the stretched exponential form of the experimental results. The parameters \( \tau \) in Eq. (1) generally represent a temperature-dependent relaxation time and \( n \) describes the deceleration in transition kinetics as it progresses. Stretched exponential magnetokinetics have been observed for Li\(_2\)(Li\(_{1-x}\)Fe\(_x\))N due to non-instantaneous magnetic moment relaxation,\(^{23}\) unlikely at the elevated temperatures used in this work. Alternatively, we can consider the \( \lambda \)-transition as a classical nucleation and growth process, described by the semi-empirical Johnson-Mehl-Avrami-Kolmogorov (JMAK) relation that takes the same form as Eq. (1). For example, the antiferromagnetic-ferromagnetic transition in FeRh has been described by a JMAK equation with \( n = 0.86.\(^{24}\) The Avrami exponent \( n \) may provide information about the nucleation and growth mechanisms.\(^{25}\) However, we believe the microscopic transition mechanism can be better described as a diffusion-limited, continuous re-ordering process akin to spinodal decomposition. As such, the FI phase grows out of the AF lattice via an augmentation in small, layer-by-layer vacancy occupancy fluctuations. A second-order transition of this type is consistent with a continuity in enthalpy \( H \) but discontinuous heat capacity \( \partial H/\partial T \) during the \( \lambda \)-transition, as measured by DSC.\(^{14}\)

Recalling the interdependence between the vacancy and magnetic structures, the simulation results thus visualize the emergence of diffuse regions of intermediate \( \Theta \) that gradually spread across other lattice points in diffuse zones rather than the formation of discrete FI nuclei (Figs. 4(a)–4(e)), also seen in Figure 4(f), where small fluctuations in layer-by-layer vacancy occupancy augment with time into an alternating-plane FI structure.

The stretched exponential fits of Eq. (1) to our measured and calculated \( \sigma(t) \) take the same form as the Kohlrausch (or KWW) function,\(^{26}\) commonly used to describe non-equilibrium dynamics in disordered condensed matter\(^{27,28}\) and diffusion in complex systems.\(^{29}\) Although generically semi-empirical, we may draw some parallels with mathematical derivations for the Kohlrausch function\(^{30}\) to suggest a more physical basis for the observed behavior. For example, a small energy distribution of energy traps may lead to deviations from “random walk” Brownian motion diffusion. Alternatively, there may be a time-dependence in populating different traps, such that relaxation occurs in stages.\(^{31}\) We dismiss the former since Brownian motion was inherently assumed in our kMC model. On the other hand, a time-decay in the rate of magnetization evolution may be more coherently explained by a combination of rapid and subordinate, slower processes. In other words, given sufficient thermal
energy cation vacancies may migrate rapidly to adjacent planes under a large thermodynamic driving force and break the magnetically compensating AF lattice symmetry. Small regions with localized FI ordering would nonetheless contribute a large increase in $\sigma$ on the scale of 10–100 s of seconds. At longer times, however, the formation of the optimal FI lattice structure for the available vacancy concentration requires a more labored rearrangement of vacancies into long-range order, slowing down the growth in $\sigma$. Only out-of-plane $V_{Fe}$ hops contribute to a rise in magnetization; however, in-plane hops continue to occur and would contribute to the lengthening of the relaxation time. We compared the ratio of out-of-plane to in-plane hops during the $\lambda$-transition in our kMC model and found that it decreased over time. Due to vacancy repulsion effects, the further the transition progresses, the lower the driving force for vacancy segregation and the smaller the probability of out-of-plane jumps.

Finally, we turn to the significance of the activation energy of 1.1 ± 0.1 eV measured by fitting the experimental $\sigma(t)$. A migration barrier for diffusion of 1.2 eV was originally cast into our kMC model based on DFT calculations. An analysis of the resulting kMC data using the same fitting procedure as for the experiment returned an apparent barrier value of 1.1 eV, confirming that the major rate-limiting step is cation diffusion. The measured activation energy includes a thermodynamic bias for the transformation on the order of 0.1 eV at 200 °C, which lowers the diffusion barrier slightly.

In conclusion, we have investigated the antiferromagnetic to ferrimagnetic $\lambda$-transition in NC-type pyrrhotites via magnetokinetic experiments and kinetic Monte Carlo simulations. In contrast to previous reports, the transformation follows a stretched exponential time-dependence. These experimental and computational results together support a description of the $\lambda$-transition as a nucleation-free, continuous reordering via diffusion on the cation sublattice. Magnetization initially rises rapidly due to small, localized displacements, but a full optimization of the ferrimagnetic superstructure is a more complex process that emerges only at longer timescales. The migration energy barrier for Fe in magnetic pyrrhotite is confirmed to be approximately 1.1 eV. The elucidation of the kinetics for this $\lambda$-transition stimulates continued studies of the rate-limiting steps of this interesting magnetic transition and the consideration of synthetic Fe$_{1-x}$S in multiferroic systems, magnetic switching, or data recording devices enabled by earth-abundant elements.

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